



GCSE MARKING SCHEME

MATHEMATICS - LINEAR

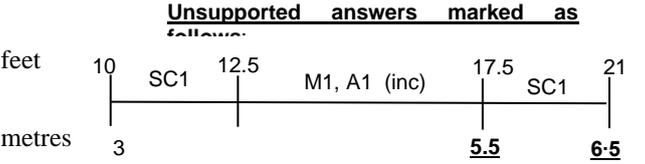
NOVEMBER 2013

INTRODUCTION

The marking schemes which follow were those used by WJEC for the November 2013 examination in GCSE Mathematics - Linear. They were finalised after detailed discussion at examiners' conferences by all the examiners involved in the assessment. The conferences were held shortly after the papers were taken so that reference could be made to the full range of candidates' responses, with photocopied scripts forming the basis of discussion. The aim of the conferences was to ensure that the marking schemes were interpreted and applied in the same way by all examiners.

It is hoped that this information will be of assistance to centres but it is recognised at the same time that, without the benefit of participation in the examiners' conferences, teachers may have different views on certain matters of detail or interpretation.

WJEC regrets that it cannot enter into any discussion or correspondence about these marking schemes.

PAPER 1 (Non calculator) Foundation Tier	Marks	FINAL MARK SCHEME Comments
4. (a) Speed of stone = $4 \times 10 + 15$ = 55 ISW (b) time = $(45 - 20)/10$ = 2.5 OR 2½ ISW	M1 A1 M1 A1 4	Correctly substituted shown by correct attempt to evaluate. For correct substitution with subtraction For example, $45 - 20/10 = 2$ gets M0,A0 Allow embedded references to the correct answer. 2 r5 gets A0
5. (a) Missing side segments = (3 and) 5 Perimeter = $3+8+3+5+3+3+3+8+3+3+8$ = 50 (cm) (b) Area = $3 \times 8 \times 2 + 3 \times 3 \times 2$ = 66 cm ²	S1 M1 A1 M1 A1 U1 6	Attempt to add ALL the correct sides of the shape Seven 3s, three 8s and a 5 (F.T. the 5 from their diagram but not 3 or 8). Watch out for implied values, e.g. 11 C.A.O. 50 should imply S1,M1,A1 F.T. their length of square from (a) Alternatively could be $2 \times 11 \times 3$ OR $11 \times 14 - 11 \times 8$ Independent of all other marks.
6. <u>any fraction equiv. to 2/5</u> (0).4 (40%) <u>any fraction equiv. to 3/10</u> (0.3) 30(%)	B1, B1 B1, B1 4	First and second values First and third values
7. (a) $3 + 3 + 1 - 2$ = 5 (b) 1 win, 1 draw and 2 losses OR WDLL $3 + 1 - 2 - 2$ (= 0) (c) (0 wins) 2 draws and 3 losses OR DDLLL $1 + 1 - 2 - 2 - 2$ (= -4)	M1 A1 B1 B1 B1 B1 6	In any order Allow 'running totals', e.g. win 3, draw 4, 2 losses = 0. In any order Answers must only use 5 games.
8. Man 5 to 7 ft OR 1.5 to 2.2 metres (both inclusive) (Man 3cm Bus = 7½cm) Scale factor = 2.5 (OR the use of 2.5 in their working) Estimate height of bus = estimate \times factor F.T. their estimates \times their SF (2 – 3 inc.) = correct answer for their figures SC1 for answers which: (a) only give man's height as 3cm and bus's as 7.5cm \pm 2mm OR (b) a proper attempt at 'dividing' the bus's height into 'man height' parts	B1 B1 M1 A1 4	<p style="text-align: center;">Unsupported answers marked as follows:</p>  <p>F.T. their man's height estimate AND scale factors 2–3 inc. Correct units must be seen at least once to get the final A1</p>
9. (a) $\angle ABD = 37^\circ$ OR $\angle DBC = 37^\circ$ $\angle A = 106^\circ$ $\angle ABD = 37^\circ$ OR $\angle BDC = 37^\circ$ $\angle C = x = 106^\circ$ $\angle C = x = 106^\circ$	B1 B1 B1	Look at diagram also C.A.O.
9. (b) $360 - 132 - 126 - 61$ = 41 (°) y = 139 (°)	M1 A1 B1 6	Angle sum of quadrilateral. Note that $180 - (360 - 126 - 132 - 61)$ is equivalent, that is $126 + 132 + 61 - 180$ For finding 4th angle. Also look in their diagram. 41 on its own gets this A1, even as $y = 41$ F.T. 'their 41'

PAPER 1 (Non calculator) Foundation Tier	Marks	FINAL MARK SCHEME Comments
<p>14. (a) Correct frequency diagram</p> <p>(b)(i) 75 (ii) Tom AND a reason, e.g. ‘more bars on left for Billy’, ‘more bars right for Tom’, ‘Tom collected more longer logs’ ‘Tom has higher number 70 – 75cm logs’, ‘Tom’s mode higher than Billy’s’</p> <p>H2</p>	<p>B2</p> <p>B1</p> <p>E1</p> <p>4</p>	<p>B1 if translated OR for at least 3 bars correct OR if height correct but slight gaps between the bars <u>If frequency polygon drawn, or indication of points at correct heights only, B0 in all cases.</u></p> <p>Accept reference to heights. Accept comparison of modal groups Do not accept Tom with statement ‘longer logs’. ‘Tom has 10 logs with length 70-75cm’, ‘Tom has highest frequency (38, Billy has 30)’</p>
<p>15.(a) 230(g) and 460(g) and 690(g) 2 and 60(ml) 320(ml) 172.5(g)</p> <p>(b) Use of 1 litre = 1000 ml or ½ litre = 500ml</p> <p>8 people needs 320ml so need $320 \div 8$ ml per person</p> <p>40 ml per person or 12.5 people</p> <p>12 portions</p> <p>H3</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>8</p>	<p>CAO CAO CAO CAO (1oz = 28.75g) If recipe for 4, treat as MR-1 (115, 230, 345: 1, 30: 160: 86.25)</p> <p>May be implied in calculation, e.g. in working towards (2cups) 480 (ml) FT ‘their 320’. throughout OR 4 people $\frac{2}{3} \times 240$ (ml) so $\frac{2}{3} \times 240 \div 4$ OR $500 \div 320$ considered or shown as repeated addition or multiplication trials towards 500</p> <p>Allow for an answer of 13 from appropriate working OR if trials or repeated addition has been used, must work to consider ‘their 320’ can be broken down into a smaller quantity per person</p> <p>(Note: FT from cream 160ml gives 25 people) Unsupported answer of 12 (people) is awarded all 4 marks</p>
<p>16. (a) 55</p> <p>(b) $2z + z + 2z + z = 24$ (or $6z = 24$ or $3z = 12$ or $2z = 24/3$) $6z = 24$ (or $z = 24/6$ or $z = 12/3$) $z = 4$</p> <p>H8</p>	<p>B2</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>5</p>	<p>B1 for evidence of $180 - (75 + 50)$ or equivalent, e.g. $360 - (105 + 125 + 75)$ incorrectly calculated, accept without brackets as intention, e.g. $180 - 75 + 50$, OR for sight of $55(^{\circ})$ or $125(^{\circ})$ from appropriate working or on the diagram</p> <p>Must be evidence of a correct equation, not $z = 4$ Do not penalise change of letter from z An answer only of ($z \equiv$) 4 without an introductory equation is M0, A0, B1. Accept answer 4 (metres) without equation <i>SCI for $z+z+z+z=24$ or $4z=24$ leading to $z=6$, or $2z+2z+2z+2z=24$ or $8z=24$ leading to $z=3$, or similar $z+2z = 24$ leading to $z = 8$ or similar</i></p>
<p>17. Realising that $\frac{1}{3}$ of the winnings is given away AND considers equivalent fractions in $\dots/24$</p> <p>8 (close friends)</p> <p>H6</p>	<p>S1</p> <p>B2</p> <p>3</p>	<p>Or sight of $\frac{1}{3} = \dots/24$ or realising $\frac{2}{3}$ is $\frac{16}{24}$ OR accept appropriate working with an amount of money</p> <p>B1 for an appropriate calculation that could lead to 8 people or 16 (left) OR sight of $\frac{16}{24}$ or $\frac{8}{24}$ Examples of calculations: $24 - 16$, or $2 \times \frac{24}{3}$ (=16 left) An unsupported correct answer is awarded all 3 marks.</p>

PAPER 1 – HIGHER TIER

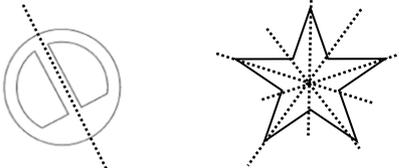
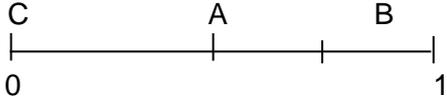
PAPER 1 Higher Tier	Marks	FINAL MARK SCHEME Comments
1(a) $\frac{(-3)^2 - 5}{2}$ $= 2$ (b) $(2 \times 5)^3$ $= 1000$ (c) $5\frac{1}{5}$ (ISW) or 5.2 or $26/5$	M1 A1 M1 A1 B2 6	Evidence of substitution. Answers of -7, $\frac{1}{2}$, -5.5 or working towards these answers is evidence of substitution (M1) Or sight of $2 \times 5 \times 2 \times 5 \times 2 \times 5$ or $10 \times 10 \times 10$ or 10^3 B1 for $5 + \frac{1}{5}$. SC1 for $-\frac{4}{5}$ from $2 - 3 + \frac{1}{5}$
2(a) Correct frequency diagram (b)(i) 75 (ii) Tom AND a reason, e.g. ‘more bars on left for Billy’, ‘more bars right for Tom’, ‘Tom collected more longer logs’, ‘Tom has higher number 70 – 75cm logs’, ‘Tom’s mode higher than Billy’s’	B2 B1 E1 4	B1 if translated OR for at least 3 bars correct OR if height correct but slight gaps between the bars If frequency polygon drawn or indication of points at correct heights, B0 in all cases Accept reference to heights. Accept comparison of modal groups Do not accept Tom with statement ‘longer logs’, ‘Tom has 10 logs with length 70-75cm’, ‘Tom has highest frequency (38, Billy has 30)’
3(a) 230(g) and 460(g) and 690(g) 2 and 60(ml) 320(ml) 172.5(g) (b) Use of 1 litre = 1000 ml or $\frac{1}{2}$ litre = 500ml 8 people needs 320ml so need $320 \div 8$ ml per person 40 ml per person or 12.5 people 12 portions	B1 B1 B1 B1 B1 M1 M1 A1 8	CAO CAO CAO CAO If recipe for 4, treat as MR-1 (115, 230, 345: 1, 30: 160: 86.25) May be implied in calculation, e.g. in working towards (2cups) 480(ml) FT ‘their 320’ throughout OR 4 people $\frac{2}{3} \times 240$ (ml) so $\frac{2}{3} \times 240 \div 4$ OR $500 \div$ ‘their 320’ considered or shown as repeated addition or multiplication trials towards 500 Allow for an answer of 13 from appropriate working OR if trials or repeated addition has been used, must work to consider how ‘their 320’ can be broken down into a smaller quantity per person (Note: FT from cream 160ml gives 25 people) Unsupported answer of 12 (people) is awarded all 4 marks
4(a) Enlargement scale factor 2 Correct position (b) Correct reflection in $y = -x$ (c) Correct rotation	B2 B1 B2 B2 7	B1 for any 3 lines correct, or consistent incorrect scale B1 for a reflection in $y = x$, OR for sight of the line $y = -x$ <i>Answer coordinates at (2, 6), (4, 6), (4, 2)</i> B1 for a ‘near miss’ slightly off the grid lines, OR 90° clockwise rotation about (-2, -4) <i>Answer coordinates at (1, -4), (1, -8), (-1, -8)</i>
5(a) $y^6 + 3y$ as a single expression (b) $2x(2x^2 - 1)$	B2 B2 4	B1 for each term. If B2 penalise further working -1 Do not accept $y \times y^5$ for y^6 . Do not accept $3 \times y$ for $3y$, Allow y^3 for $3y$ B1 for correct but only partially factorised OR $2x(2x^2 \dots)$ or $2x(\dots -1)$
6. Realising that $\frac{1}{3}$ of the winnings is given away AND considers equivalent fractions in $\dots/24$ 8 (close friends)	S1 B2 3	Or sight of $\frac{1}{3} = \dots/24$ or realising $\frac{2}{3}$ is $16/24$ OR accept appropriate working with an amount of money B1 for an appropriate calculation that could lead to 8 people or 16 (left) OR sight of $16/24$ or $8/24$ Examples of calculations: $24 - 16$, or $2 \times 24/3$ (=16 left) An unsupported correct answer is awarded all 3 marks.

PAPER 1 Higher Tier	Marks	FINAL MARK SCHEME Comments
<p>7. (Ratio bonus) (1 share) (£)2500÷5 (2 shares is $500 \times 2 =$) (£)1000 (Percentage option) (6% of £17000 =) $0.06 \times (\text{£})17000 = (\text{£})1020$</p> <p>Valid reason based on working, e.g. '6% option because it is more money', or '6% option as it is £20 more'</p> <p>Look for</p> <ul style="list-style-type: none"> • spelling • clarity of text explanations, • the use of notation (watch for the use of '=', £, p) <p>QWC2: Candidates will be expected to</p> <ul style="list-style-type: none"> • present work clearly, maybe with diagrams and words explaining process or steps <p>AND</p> <ul style="list-style-type: none"> • make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer <p>QWC1: Candidates will be expected to</p> <ul style="list-style-type: none"> • present work clearly, maybe with diagrams and words explaining process or steps <p>OR</p> <ul style="list-style-type: none"> • make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer 	<p>M1 A1 M1 A1 E1</p> <p>QWC 2</p> <p>7</p>	<p>Alternative method to find 1% ($\div 100$) then 6% ($\times 6$)</p> <p>FT from their two values provided both M marks awarded, must be based on two values to compare</p> <p>QWC2 Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.</p> <p>QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar</p> <p>OR</p> <p>evident weaknesses in organisation of material but using acceptable mathematical form, with few if any errors in spelling, punctuation and grammar.</p> <p>QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling, punctuation or grammar.</p>
<p>8(a) 55</p> <p>(b) $2z + z + 2z + z = 24$ (or $6z = 24$ or $3z = 12$ or $2z = 24/3$)</p> <p style="text-align: center;">$6z = 24$ (or $z = 24/6$ or $z = 12/3$) (z=) 4 (metres)</p>	<p>B2</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>5</p>	<p>B1 for evidence of $180 - (75 + 50)$ or equivalent, e.g. $360 - (105 + 125 + 75)$ incorrectly calculated, accept without brackets as intention, e.g. $180 - 75 + 50$, OR for sight of 55° or 125° from appropriate working or on the diagram</p> <p>Must be evidence of a correct equation, not $z = 4$</p> <p>Do not penalise change of letter from z</p> <p>An answer only ($z =$) 4 without an introductory equation is M0, A0, B1. Accept answer 4 (metres) without equation</p> <p>SC1 for $z + z + z + z = 24$ or $4z = 24$ leading to $z = 6$, or $2z + 2z + 2z + 2z = 24$ or $8z = 24$ leading to $z = 3$, $z + 2z = 24$ leading to $z = 8$ or similar</p>
<p>9(a) Selecting $8y = -3x + 12$</p> <p>Either shows $y = -(1.5/4)x + 1.5$ or shows trials, within $8y = -3x + 12$ knowing that (0, 1.5) or (-4, 3) and (4, 0) lie on this line</p> <p>or appropriate elimination of all other equations</p> <p>(b) $(2 + -2)/2$ or $(-4 + 6)/2$</p> <p style="text-align: center;">(0, 1)</p>	<p>B1</p> <p>E1</p> <p>M1</p> <p>A1</p> <p>4</p>	<p>SC1 for selection of $8y = 3x + 12$ with some attempt at a reason (e.g. elimination of other equations)</p> <p>Do not accept 'the one that works' without saying why?</p> <p>Do not accept 'negative gradient', as this is insufficient</p> <p>OR attempt sketch with reasonable idea of mid point (not when giving intersection as a response)</p> <p>Watch for, and accept the use of (a) graph paper</p> <p>(Watch for (0,2) without working or from incorrect working this is M0, A0)</p>
<p>10(a) 5, 16, 33</p> <p>(b) -50</p> <p>(c) $n^2 - 10$</p>	<p>B2</p> <p>B1</p> <p>B2</p> <p>5</p>	<p>Ignore any further values given</p> <p>B1 for 2 correct terms in the correct position</p> <p>SC1 for 0, 5, 16 or ..., 5, 16, 33</p> <p>CAO</p> <p>Mark final answer</p> <p>B1 for $n^2 \pm \dots$, not for n^2 alone, written within an expression of at least 2 terms</p> <p>B0 for $an^2 \pm \dots$ where $a \neq 1$</p>

PAPER 1 Higher Tier	Marks	FINAL MARK SCHEME Comments
11(a) (£)220 (b) 220×1.03 (£)226.6(0)	B1 M1 A1 3	FT 'their 220' from (a) Alternatively finding 3% and adding to 220 CAO. ISW
12(a) $(x + 3)(x - 7)$ $x = -3$ and $x = 7$ (b) $2(2x + 3) + 3(4x + 1) = 129$ $16x + 9 = 129$ $x = 120/16 (=7.5)$ (c) $2d + de = 15 - 3e$ $de + 3e = 15 - 2d$ $e(d + 3) = 15 - 2d$ $e = \frac{15 - 2d}{d + 3}$	B2 B1 M2 A1 A1 B1 B1 B1 B1 11	B1 for $(x - 3)(x + 7)$ or $x(x - 7) + 3(x - 7)$ or equivalent FT from their pair of brackets, or from previous B1 Do not accept answer only, must FT from factorising For correctly clearing all 3 fractions, OR M1 for clearing 2 fractions FT from M1 Accept 240/32. Ignore incorrect cancelling SC1 provided no other marks awarded for $\frac{16x + 9}{6} (= \frac{129}{6})$ FT until 2 nd error for equivalent level of difficulty Mark final answer
13. Shows understanding of the distance PQ around the cylinder, as straight line $PQ^2 = \text{circumference}^2 + h^2$ $PQ^2 = (2\pi r)^2 + h^2$ (PQ =) $\sqrt{(2\pi r)^2 + h^2}$ or $\sqrt{4\pi^2 r^2 + h^2}$	S1 M1 A1 A1 4	E.g. shows a rectangle with PQ as the diagonal Allow split into 2 diagonals straight lines Allow application of Pythagoras' Theorem as FT from a split into 2 diagonals Accept $PQ^2 = 2\pi r^2 + h^2$ as idea for method No further FT from split diagonals
14. 12.5(kg)	B2 2	B1 for sight of 2.5(kg)
15(a) -16 and -8 (b) At least 4 points plotted accurately All 9 points plotted accurately and joined with a curve (c) (0, 0) (2, -16) or follow through from their graph (d) $y = 8 - 8x$ drawn accurately and intersecting the curve Coordinates of the point of intersection	B1 M1 A1 B1 M1 A1 6	FT from (a) Plots reasonable for the scale and the intention for the curve to pass through all of the points plotted Need both points where gradient is zero FT from consistent misread of the scale if possible FT from their curve if possible Reasonable for their graphs, reading accurate to gridlines Accept with missing brackets Accept unsupported answers (2.5, -12.5) to (2.5, -12)
16(a) Attempt to find the difference between $100x = 34.2727\dots$ and $x = 0.342727\dots$ $3393/9900$ (b) Any 3 correct responses, e.g. 0, $\frac{1}{4}$, $\frac{1}{9}$, 1, 4, 9, 16, 25,.. (c)(i) Correct response, e.g. $\sqrt{2}$, $\sqrt{3}$, $\sqrt{\frac{1}{2}}$, $\sqrt{5}$, $\sqrt{21}$, .. (ii) Correct response, e.g. π , $\sqrt{\pi}$, ${}_3\sqrt{2}$, ${}_5\sqrt{7}$, ... (d) $(\sqrt{2 \times 16} + \sqrt{2})^2$ $(4\sqrt{2} + \sqrt{2})^2 (= (5\sqrt{2})^2)$ 50	M1 A1 B2 B1 B1 M1 A1 A1 9	Or differences with correct values for 10000x and 100x, or 1000x and 10x, or alternative full method, or sight of 33.93/99, 339.3/990 ISW Accept if consistently written with index 3/2 Accept if more than 3 responses offered if all are correct B1 for any 2 correct responses with no more than 1 incorrect response If an incorrect response offered with a correct response, B0 Do not accept $\sqrt{\pi}$ OR M1 $32 + \sqrt{32}\sqrt{2} + \sqrt{32}\sqrt{2} + 2$ any 3 terms correct A1 $32 + 8 + 8 + 2$ CAO A1 50
17(a) Strategy, finding area $0.2 \times 30 + 0.4 \times 10 + 0.8 \times 10 + 1.2 \times 10 + 1.0 \times 10 + 0.1 \times 30$ 43 (people) (b) $6 + 4 + 8 + 12 + \frac{1}{2} \times 10$ OR $43 - 3 - \frac{1}{2} \times 10$ 35 (people)	M1 M1 A1 M1 A1 5	Any single area is sufficient (Note for markers: 6+4+8+12+10+3) CAO FT 'their 43'

PAPER 1 Higher Tier	Marks	FINAL MARK SCHEME Comments
<p>18(a) P(not purple, not purple) with sight of $6/8$ OR sight of an alternative full strategy</p> <p style="text-align: center;">$6/8 \times 5/7$ or alternative full calculation shown 30/56 ISW (15/28)</p> <p>(b) $P(RR)+P(PP)+P(BB)+P(WW)$</p> <p>Sight of $2/8 \times 1/7$ in appropriate working $4 \times (2/8 \times 1/7)$ or equivalent 1/7</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>7</p>	<p>Not for sight of $6/8$ alone, i.e. as 6 non purple shoes out of 8 shoes Allow B1 for sight of $6/8 \times 5/8$</p> <p>OR $1 - P(2 \text{ different colours})$ OR $P(\text{any shoe}) \times P(\text{its matching shoe})$</p> <p>OR $8/8 \times 1/7$ OR $8/8 \times 1/7$ OR equivalent fraction</p>

PAPER 2 – FOUNDATION

PAPER 2 (Calculator allowed) Foundation Tier	Marks	FINAL MARK SCHEME Comments																				
<p>1. (a) (59.96) 32.7(0) (socks) 55.38 (shirts) 65.36 (shoes)</p> <p>(£) 213.4(0)</p> <p>(b) 10% = 21.34 5% = 10.67 OR (0).05 × 213.4(0) Discount = (£) 10.67</p>	<p>B1 B1 B1 B1 M1 A1 6</p>	<p>F.T. their figures for 1 error If cost of shirts is £110.76 then total would be (£)268.78 and discount is (£)13.439 OR (£)13.44 OR (£)13.43 For any correct method for finding 5% F.T. their total. Allow M1,A1 for (£)202.73 OR (£)255.34 Also FT 95% of their total. 1% = 2.13 then 5% = 10.65 M1 A1 PA-1</p>																				
<p>2.</p> <table border="0"> <tr> <td>Distance</td> <td>160mm</td> <td>160cm</td> <td>160m</td> <td>160km</td> </tr> <tr> <td>Weight</td> <td>35kg</td> <td>350kg</td> <td>35mg</td> <td>35g</td> </tr> <tr> <td>Capacity</td> <td>35 litres</td> <td>350litres</td> <td>350 ml</td> <td>35 mm³</td> </tr> <tr> <td>Height</td> <td>1900cm</td> <td>190cm</td> <td>19cm</td> <td>190mm</td> </tr> </table>	Distance	160mm	160cm	160m	160km	Weight	35kg	350kg	35mg	35g	Capacity	35 litres	350litres	350 ml	35 mm ³	Height	1900cm	190cm	19cm	190mm	<p>B1 B1 B1 B1 4</p>	
Distance	160mm	160cm	160m	160km																		
Weight	35kg	350kg	35mg	35g																		
Capacity	35 litres	350litres	350 ml	35 mm ³																		
Height	1900cm	190cm	19cm	190mm																		
<p>3. (a) Evidence of square counting 59 – 65</p> <p>3. (b)</p> 	<p>M1 A1 B1 B1 4</p>	<p>Condone square notation, e.g. 60², but 60² = 3600 gets A0</p> <p>Circles: for the 1 correct line and no other Star: for all 5 correct lines</p>																				
<p>4. (a)</p>  <p>(b) likely</p>	<p>B1 B1 B1 B1 4</p>	<p>A should be at 1/2. Condone use of W(hite) B should be between 3/4 and 1 exclusive. (3/4 is to the right of the 'e' in 'red'. Welsh scripts: To the right of the final 'o' in 'stopio') Condone use of Y(ellow) C should be at 0. Condone use of R(ed) Letters must be seen on scale (i.e. not 0.5, 0.875 and 0) C.A.O.</p>																				
<p>5. (a) (i) cylinder</p> <p>(ii) cuboid</p> <p>(b) tangent</p> <p>(c) Perpendicular through C</p>	<p>B1 B1 B1 B1 4</p>	<p>Accept 'circular based cylinder', 'cylindrical prism', 'cylinder prism', but not 'circular prism' Accept 'rectangular cuboid', but not 'rectangular prism'</p> <p>Tolerance: Between a line to the right of 'B' in AB and a line to left of the 'p' in passes (inclusive) On Welsh script between a line to the right of 'l' in perpendicwlar and a line to left of the 's' in sy'n (inclusive)</p>																				

PAPER 2 (Calculator allowed) Foundation Tier	Marks	FINAL MARK SCHEME Comments
6. (a) (£)3.16 (b) (£)9.2(0)	B1 B1	
<p>6. (c) 5 (£)1.28 × 5 (6.40) + (£)27.46 = (£)33.86 (Change =) (£)6.14</p> <p>QWC Look for</p> <ul style="list-style-type: none"> • Spelling • Clarity of text explanations • The use of notation – watch for ‘=’, ‘£’, ‘p’ being used appropriately. <p>QWC2: Candidates will be expected to</p> <ul style="list-style-type: none"> • present work clearly, with words explaining their processes or steps <p>AND</p> <ul style="list-style-type: none"> • make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer <p>QWC1: Candidates will be expected to</p> <ul style="list-style-type: none"> • present work clearly, with words explaining their processes or steps <p>OR make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer</p>	<p>B1 M2 A1 A1</p> <p>QWC 2</p> <p>9</p>	<p>M1 for 27.46 +..... OR 1.28 × 5 +</p> <p>F.T. (£)32.58 from (£)1.28 × 4 (5.12) + (£)27.46</p> <p>FT provided M1 awarded</p> <p>Penalise –1 for consistent use of incorrect column.</p> <p><u>UK and Europe: (£)13.82 + 5×60(p) (16.82) (£)23.18</u></p> <p><u>World Zone 1 : (£)26.28 + 5×1.22 (32.38) ((£)7.62</u></p> <p>QWC2 Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.</p> <p>QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar.</p> <p>OR</p> <p>Evident weaknesses in organisation of material but using acceptable mathematical form, with few if any errors in spelling, punctuation and grammar.</p> <p>QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling</p>
<p>7. (a) 101</p> <p>(b) $2 \times 60 + 1$ OR <u>60+61</u> = 121</p> <p>(c) $(81 - 1)/2$ = 40</p>	<p>B1</p> <p>M1 A1</p> <p>M1 A1 5</p>	<p><u>C.A.O. 40+41; 40,41; 40 unshaded get M1, A0.</u></p>
<p>8. (a) (i) Add 12 to the previous term</p> <p>(ii) Multiply the previous term by –3</p> <p>(b) $F = 6(12) + 10(3)$ OR $72 + 30$ = 102</p> <p>(c) (i) 8m (ii) (£) 8m/100 OR (£)(0).08m</p>	<p>B1</p> <p>B1</p> <p>M1 A1</p> <p>B1 B1</p> <p>6</p>	<p>Accept +12, <u>goes up in 12s, but 12n–8 is B0</u></p> <p>Accept ×–3.</p> <p><u>Multiply by 3 and alternate (or change) sign gets B1.</u></p> <p>For correct substitution <u>and correct interpretation</u></p> <p>C.A.O.</p> <p>Accept $8 \times m$, $m \times 8$, $m8$</p> <p>F.T. 'their (c)(i) <u>if algebraic</u></p> <p><u>Penalise –1 once for use of different letter but allow M</u></p> <p><u>Use of the letter p gets B0 every time.</u></p>
<p>9. (a) Sum of the numbers (476) Sum/8 $59 \cdot 5$<u>(0)</u> I.S.W.</p> <p>(b) 27</p> <p>(c) 45 45 55 <u>59 65</u> 66 69 72</p> <p>Median = 62</p>	<p>M1 M1 A1</p> <p>B1</p> <p>M1 A1 6</p>	<p>For attempt to add the numbers</p> <p>For dividing a number in the range 400 – 550 by 8.</p> <p>C.A.O.</p> <p><u>–27 gets B0.</u></p> <p>For identifying the correct TWO middle numbers OR for arranging the 8 numbers in ascending or descending order.</p> <p>C.A.O.</p> <p>Unsupported 62 gets M1, A1.</p>

PAPER 2 (Calculator allowed) Foundation Tier	Marks	FINAL MARK SCHEME Comments	
10. (a) 114 (miles) (b) 64 (miles) (c) 42 (minutes) (d) Line drawn from end of stopping to (13:39, 0)	B1 B1 B1 B1 4	F.T. 'their 114' – 50 Three 2mm squares beyond 13:30 on the time axis. <u>(Accuracy of ½ small square)</u>	
11. (a) $\frac{95}{250} \times 100$ 38 (%) (b) $((£) 163.60 - (£) 35.60) = (£) 128$ Number of extra days = <u>'their (£)128' / (£)16</u> = 8 Total number of days = 10	M1 A1 B1 M1 A1 B1 6	For the (£)128 F.T. except for (£)163.60/(£)16 Unsupported 10 gets all 4 marks. F.T. number of extra days + 2 <u>Answers like '2 days and a further 8 days' get B0</u> <u>Subtracting two lots of £35.60 gets B0 for first B mark. But can then get M1,A1 on correct F.T. even if their answer is not a whole number. In such cases the final B1 is only awarded if their number of days is rounded up to the next whole number.</u> <u>Watch out for $163.60/16 = 10.2 = 10$ (days) which gets 0.</u>	
12. <u>Either</u> He spends (£)100 on rent and (£)160 on food leaving (£)140 F.T. for second M1,A1 Frac. remaining 140/400 7/20 I.S.W.	OR $\frac{1}{4} + \frac{2}{5}$ = 13/20 F.T. for second M1,A1 Frac. remaining = $1 - \frac{13}{20}$ = 7/20 I.S.W.	M1 A1 M1 A1 4	<u>Subtracting at each stage :</u> <u>Spends (£)100 on rent</u> <u>Leaving £300. 2/5 of £300 = 120 leaving (£)180</u> F.T. for second M1,A1 <u>Frac. remaining 180/400 = 9/20</u> <u>Possible 4 marks then –1 if any A marks awarded</u> <u>Decimals or % equivalents</u> <u>.25 + .4(0) = .65.</u> <u>1- .65 = .35</u> <u>First M1, A1 possible</u> <u>F.T. for second M1,A1 but must be fractions for second M1,A1.</u> <u>35/100 M1</u> <u>= 7/20 A1</u>
13. (a) $\hat{PQR} = 48^\circ$ $\hat{PRQ} = 67^\circ$. Completed triangle (b) First arc(s) Final arcs and line (c) First arc(s) Final arc(s) and line	B1 B1 B1 B1 B1 B1 7	<u>If triangle is 'flipped' then mark as if correct then –1</u> Provided at least B1 awarded If no arcs then B0, B0 <u>Arc must be big enough so that the 2nd arc could cut it</u> <u>B2 for correct construction at A</u> <u>B1 maximum for a correct construction elsewhere on the line.</u>	
14. <u>Accept angles shown on their diagram</u> $\hat{BCE} = 60^\circ$ OR $\hat{HCG} = 60^\circ$ $\hat{ECG} = 90^\circ$ OR $\hat{DCB} = 90^\circ$ <u>Accept the 'box' notation</u> $\hat{DCH} = 360^\circ - 60^\circ - 60^\circ - 90^\circ - 90^\circ$ = 60° DC = CH <u>(OR marked as equal on the diagram with $\hat{DCH} = 60^\circ$)</u>	B1 B1 M1 A1 E1 5	For at least one correct 60° (<u>Anywhere in either triangle</u>) For at least one correct 90° (<u>Anywhere in either square</u>) Angles at a point make 360 $\hat{DCH} = 60$ <u>on its own gets no marks.</u> <u>Needs to show having the 60° and DC = CH.</u>	

PAPER 2 (Calculator allowed) Foundation Tier	Marks	FINAL MARK SCHEME Comments
15.(Agatha) 220, 440, 660, (880, 1100, 1320, ...) (p) (Ben) 140, 280, 420, (560, 700, 840, 980, ...) (p) $4 \times 2(.)20 = 8(.)80$ AND $3 \times 1(.)40 = 4(.)20$ (£ or p) 7 (pens) OR $3.60, 7.20, 10.80, (14.40 \dots) + 2.20$ $4 + 3$ 7 H1	M1 M1 A1 A1 M1M1 A1 A1 4	In £ or p or mixed. M1 for the any 3 correct multiples In £ or p or mixed. M1 for the any 3 correct multiples Identifying the correct number of each CAO. Must state total number of pens altogether <i>Alternative, Trial & improvement:</i> 2 trials, correctly evaluated showing improvement M1 2 trials, correctly evaluated between £10 & £16 incl. M1 $4 \times 2(.)20$ and $3 \times 1(.)40 = (£)13$ A1 $7(\text{pens})$ CAO A1 Award all 4 marks for an unsupported answer of 7 (pens)
16. (a) 3.8 (cm) or states 'the same' Reason, e.g. 'they even out', 'the mean of these is zero', 'totals are the same each week', 'taking away 3 and adding 3 so it stays the same', 'same amount of rainfall in both weeks' (b)(i) Mid-points 1, 2, 3, 4 $1 \times 5 + 2 \times 11 + 3 \times 13 + 4 \times 1$ Intention their $\sum fx / 30$ $2.3(33\dots\text{cm})$ (ii) Modal class $2.5 \leq r < 3.5$ (13) (iii) Median $1.5 \leq r < 2.5$ H4	B1 E1 B1 M1 m1 A1 B1 B1 8	Mark final answer. Award independently from E mark Accept a correct method as a reason, e.g. $(3.8 \times 7 + 3 - 3) \div 7$ or equivalent Allow '3.8+3 = 6.8, and 6.8-3 = 3.8', or $4.8 \times 3 + 2.8 \times 3 + 3.8 = 26.6$ with $26.6 \div 7 = 3.8$ i.e. showing by calculation that +3 and -3 means no change. Allow indication of +1 -1 bringing 3.8 or 7×3.8 back to original FT their mid points, including bounds, provided they fall within the classes. $5 + 22 + 39 + 4 (= 70)$ (70/30) Following correct working, however accept unsupported $2.3(3\dots\text{cm})$ for all 4 marks. Accept 7/3 or $2\frac{1}{3}$ as a final answer Accept '2.5 to 3.5' (with/without '13') Accept '1.5 to 2.5' <i>If neither B1 awarded in (ii) or (iii), then award SC1 for answers of 3 and 2 respectively.</i>
17. (a)(i) 200×1.09137 OR $200 \div 0.916279$ $218(.274)$ (ii) 250×1.4789 OR $250 \div 0.676175$ $369(.72\dots)$ (b) $1 \div 133.5$ or $1 \div 0.090147$ $0.0074\dots\dots$ 11.09 H5	M1 A1 M1 A1 M1 A1 A1 7	Accept $200 \times 1.09(\dots)$ and same with other calculations Accept rounded or truncated Accept unambiguous truncation Accept rounded or truncated, also accept 370 Sight of either calculation Either answer correctly placed in the table also implies M1 Accept 0.0075. Only allow 0.01 if correct working seen If answers reversed in the table award M1, A0, A1 If 2 correct answers seen in working award M1, A1, A0 If 1 correct answer seen in working award M1, A0, A0 If only 1 answer given misplaced in table award M1, A0, A0
18. (a) $6 \times \dots = 54$ or $54 \div 6 = \dots$ (Area each face on small cube =) $9(\text{cm}^2)$ 18 (small faces on cuboid) $(18 \times 9 =) 162(\text{cm}^2)$ (b) (Length side of small cube =) $\sqrt[3]{9}$ (= 3) Volume = $(4 \times) 3 \times 3 \times 3$ $108(\text{cm}^3)$ H8	M1 A1 B1 B1 M1 m1 A1 7	ISW. Watch for an embedded answer. FT 'their $54 \div 6$ ' \times 'their 18' evaluated correctly from a consistent misconception of the number of faces. Alternative: $Single\ cube\ has\ 6\ faces$ B1 $Cuboid\ has\ 18\ faces$ B1 $Total\ surface\ area\ 3 \times 54$ M1 $\dots\dots\dots = 162(\text{cm}^2)$ A1 OR $6\ hidden\ faces$ B1 $Equivalent\ to\ 3\ cubes\ at\ 6\ faces\ each$ B1 $Total\ surface\ area\ 3 \times 54$ M1 $\dots\dots\dots = 162(\text{cm}^2)$ A1 OR $Area\ 4\ cubes\ 4 \times 54 = 216$ B1 $6\ hidden\ faces$ B1 $Area\ of\ cuboid\ 216 - 54$ M1 $\dots\dots\dots = 162(\text{cm}^2)$ A1 FT 'their 9' provided M1 awarded in (a) Method to calculate volume of 1 or 4 cubes. FT 'their 3' provided M1 awarded These alternatives are only marked AS COMPLETE SOLUTIONS. You must not award credit for any of the individual lines. For example, Area 4 cubes $4 \times 54 = 216$. On its own this gets B0. It only gets B1 as a part of a complete solution with all the other lines for that alternative

PAPER 2 HIGHER TIER

PAPER 2 Higher Tier	Marks	FINAL MARK SCHEME Comments
<p>1.(Agatha) 220, 440, 660, (880, 1100, 1320, ...) (p) (Bryn) 140, 280, 420, (560, 700, 840, 980, ...) (p) $4 \times 2(.)20 = 8(.)80$ AND $3 \times 1(.)40 = 4(.)20$ (£ or p) 7 (pens)</p>	<p>M1 M1 A1 A1</p> <p align="center">4</p>	<p>In £ or p or mixed. M1 for any 3 correct multiples In £ or p or mixed. M1 for any 3 correct multiples Identifying the correct number of each CAO. Must state total number of pens altogether <i>Alternative, Trial & improvement:</i> <i>2 trials, correctly evaluated showing improvement</i> M1 <i>2 trials, correctly evaluated between £10 & £16 inclusive</i> M1 $4 \times 2(.)20$ and $3 \times 1(.)40 = (£)13$ A1 7(pens) CAO A1</p> <p>Award all 4 marks for an unsupported answer of 7 (pens)</p>
<p>2(a) $(12 - 2) \times 180$ $\div 12$ $150(^{\circ})$</p> <p>(b) No AND a reason, e.g. '150 not a factor or 360', '150+150 = 300 not enough', '3 lots of 150 is 450 too much'</p>	<p>M1 m1 A1</p> <p>E1</p> <p align="center">4</p>	<p>Alternative: Sum of exterior angles $360(^{\circ})$ Exterior $360/12$ (not as a final answer) Interior $(180 - \text{exterior}) 150(^{\circ})$ <i>If final answer 360/12 or 30, then allow M1, m0, A0</i> OR <i>Sum interior</i> $((2 \times 12 - 4) \text{ rt angles}) 20 \times 90(^{\circ}) (= 1800(^{\circ}))$ M1 <i>Each interior angle</i> $(1800) \div 12$ m1 $150(^{\circ})$ A1</p> <p>No FT from working with exterior angle in (a), FT from M1, m1 in (a) only</p>
<p>3(a)(i) $-13g + 4h$</p> <p>(ii) $15p^{11}$ (iii) $2y^4$ (b) $3 \times x + 4 \times 2x$ or equivalent $11x$</p>	<p>B2</p> <p>B1 B1 B1 B1</p> <p align="center">6</p>	<p>Must be written as an expression. B1 for either term correct Mark final answer ISW ISW (ii) & (iii) penalise change of variable once only -1 Mark final answer. FT for equivalent level of difficulty, provided either pencils or pens is correct</p>
<p>4(a) 3.8 (cm) or states 'the same' Reason, e.g. 'they even out', 'the mean of these is zero', 'totals are the same each week', 'taking away 3 and adding 3 so it stays the same', 'same amount of rainfall in both weeks'</p> <p>(b)(i) Mid-points 1, 2, 3, 4 $1 \times 5 + 2 \times 11 + 3 \times 13 + 4 \times 1$ Intention their $\sum fx / 30$ $2.3(33 \dots \text{cm})$</p> <p>(ii) Modal class $2.5 \leq r < 3.5$ (iii) Median $1.5 \leq r < 2.5$</p>	<p>B1 E1</p> <p>B1 M1 m1 A1</p> <p>B1 B1</p> <p align="center">8</p>	<p>Mark final answer. Award independently from E mark Accept a correct method as a reason, e.g. $(3.8 \times 7 + 3 - 3) \div 7$ or equivalent Allow '3.8+3 = 6.8, and 6.8-3 = 3.8', or '4.8×3+2.8×3 + 3.8 = 26.6 with 26.6÷7=3.8 i.e. showing by calculation that +3 and -3 means no change. Allow indication of + 1 -1 bringing 3.8 or 7×3.8 back to original</p> <p>FT their mid points, including bounds, provided they fall within the classes. $5 + 22 + 39 + 4 (= 70)$ $(70/30)$ Following correct working, however accept unsupported $2.3(3 \dots \text{cm})$ for all 4 marks. Accept $7/3$ or $2\frac{1}{3}$ as a final answer Accept '2.5 to 3.5' Accept '1.5 to 2.5' <i>If neither B1 awarded in (ii) or (iii), then award SCI for answers of 3 and 2 respectively.</i></p>

PAPER 2 Higher Tier	Marks	FINAL MARK SCHEME Comments
<p>8(a) $6 \times \dots = 54$ or $54 \div 6 = \dots$ (Area each face on small cube =) $9(\text{cm}^2)$ 18 (small faces on cuboid) ($18 \times 9 =$) $162(\text{cm}^2)$</p> <p>Look for</p> <ul style="list-style-type: none"> • spelling • clarity of text explanations, • the use of notation (watch for the use of '=', cm^2) <p>QWC2: Candidates will be expected to</p> <ul style="list-style-type: none"> • present work clearly, with words explaining process or steps <p>AND</p> <ul style="list-style-type: none"> • make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer <p>QWC1: Candidates will be expected to</p> <ul style="list-style-type: none"> • present work clearly, with words explaining process or steps <p>OR</p> <ul style="list-style-type: none"> • make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer <p>(b) (Length side of small cube =) $\sqrt[3]{9}$ (= 3) Volume = $(4 \times 3 \times 3 \times 3)$ $108 (\text{cm}^3)$</p>	<p>M1 A1 B1 B1</p> <p>QWC 2</p> <p>M1 m1 A1 9</p>	<p>ISW. Watch for an embedded answer. FT 'their $54 \div 6$' \times 'their 18' evaluated correctly from a consistent misconception of the number of faces.</p> <p><i>Alternative:</i> Single cube has 6 faces Cuboid has 18 faces Total surface area 3×54 $= 162 (\text{cm}^2)$</p> <p>OR 6 hidden faces Equivalent to 3 cubes at 6 faces each Total surface area 3×54 $= 162 (\text{cm}^2)$</p> <p>OR Area 4 cubes $4 \times 54 = 216$ 6 hidden faces Area of cuboid $216 - 54$ $= 162 (\text{cm}^2)$</p> <p>QWC2 Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.</p> <p>QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar OR evident weaknesses in organisation of material but using acceptable mathematical form, with few if any errors in spelling, punctuation and grammar.</p> <p>QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling, punctuation or grammar.</p> <p>FT 'their 9' provided M1 awarded in (a) Method to calculate volume of 1 or 4 cubes. FT 'their 3' provided M1 awarded</p>
<p>9(a) 1.26×120 OR $0.26 \times 120 + 120$ (£)151.2(0) (b) $43.55/0.65$ OR $(43.55/65) \times 100$ 67 (m)</p>	<p>M2 A1 M1 A1 5</p>	<p>M1 for 0.26×120 (=31.2(0)) Mark final answer</p> <p>ISW (e.g. attempt to change units)</p>
<p>10. Any 2 of the lines $x+y=4$, $y=2x+4$ and $y=1$ correct Correct region shaded</p>	<p>B2 B1 3</p>	<p>B1 for any 1 correct line CAO</p>

PAPER 2 Higher Tier	Marks	FINAL MARK SCHEME Comments
17. Strategy, information transferred to the diagram with D marked on BC, AND deciding need to find AB using sine rule then need to find AD using cosine rule $AB/\sin 60^\circ = 10.6/\sin 35^\circ$ $AB = \sin 60^\circ \times 10.6/\sin 35^\circ$ (Rearranged form implies M1) $AB = 16(.0046\dots \text{cm})$ (FT their AB within cosine rule, not use of 10.6) $AD^2 = 14.2^2 + AB^2 - 2 \times 14.2 \times AB \times \cos 35^\circ$ $AD^2 = 85.4(576\dots)$ $AD = 9.2(443\dots \text{cm})$ rounded or truncated from correct working	S1 M1 A1 A1 M1 A1 A1 7	<i>Alternative example:</i> <i>Strategy, information transferred to the diagram with D marked on BC, AND deciding need to find BC using sine rule, then $DC=BC-BD$, then need to find AD using cosine rule</i> $BC/\sin 85^\circ = 10.6/\sin 35^\circ$ $BC = \sin 85^\circ \times 10.6/\sin 35^\circ$ (Rearranged form implies M1) $BC = 18.4(102\dots \text{cm})$ AND $DC(BDC - 14.2) = 4.2(102\dots \text{cm})$ (FT their DC within cosine rule, not use of 14.2) $AD^2 = 10.6^2 + DC^2 - 2 \times 10.6 \times DC \times \cos 60^\circ$ $AD^2 = 85.4(576\dots)$ $AD = 9.2(443\dots \text{cm})$ rounded or truncated from correct working
18. $\Pi \times 4.6^2 \times 93/360$ Answers between 17.16 and 17.18 or 17.2 (cm ²) Appropriate use of $\frac{1}{2} ab \sin C$ OR $\cos 46.5 = h/4.6$ with $\sin 46.5 = b/4.6$ $\frac{1}{2} \times 4.6 \times 4.6 \times \sin 93$ OR $h = 3.16643\dots$ and $b = 3.3367\dots$ (Triangle area) 10.5655...(cm ²) Approximately 6.6 (cm ²)	M1 A1 M1 M1 A1 B1 6	Method to find base & height of right angled triangle Needs to be height and $\frac{1}{2}$ base or base evaluated Do not accept 10.5 (cm ²) Depends on at least M1 from attempt to find each area, then FT their difference in areas



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