



GCSE MARKING SCHEME

MATHEMATICS 2-TIER

SUMMER 2010

INTRODUCTION

The marking schemes which follow were those used by WJEC for the Summer 2010 examination in GCSE MATHEMATICS - 2-TIER. They were finalised after detailed discussion at examiners' conferences by all the examiners involved in the assessment. The conferences were held shortly after the papers were taken so that reference could be made to the full range of candidates' responses, with photocopied scripts forming the basis of discussion. The aim of the conferences was to ensure that the marking schemes were interpreted and applied in the same way by all examiners.

It is hoped that this information will be of assistance to centres but it is recognised at the same time that, without the benefit of participation in the examiners' conferences, teachers may have different views on certain matters of detail or interpretation.

WJEC regrets that it cannot enter into any discussion or correspondence about these marking schemes.

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Mathematics Paper 1 - Foundation Tier

Paper 1 (Non calculator) -Foundation Tier Summer 2010	✓	Marks	Comments
1. (a) (i) 12314 (ii) Six hundred and fifty one thousand three hundred		B1 B1	C.A.O. C.A.O.
1. (b) (i) 43 and 47 (ii) 12 and 37 (iii) 55 (iv) 16		B1 B1 B1 B1	In either order In either order C.A.O. C.A.O.
1. (c) 6580		B1	C.A.O.
1. (d) 30 (%)		B1	C.A.O.
1. (e) 1, 35, 5, 7		B2	B1 for any 2 OR 3 factors and no incorrect numbers. OR the 4 correct factors and 1 incorrect number.
2. (a) (i) 32 (ii) 66		B1 B1	C.A.O. C.A.O.
2. (b) (0)·7(0) (0)·75 ·7(0) or 70% ·73 ·75 or $\frac{3}{4}$		B1 B1 B1	C.A.O. C.A.O. If no answer offered on the dotted lines, allow the first two B1s if (0)·7 and/or (0)·75 seen in subsequent work. F.T. their values.
3. (Viewed with diagram) Attempt to count squares 62 – 70 cm ²		M1 A1 U1	Within the range inclusive Independent of the other marks Answers such as 65 ² get M1, A1, U0
4. (a) Overlay Point E so that DE = 9·8 (cm)		B1	Inclusive bounds are shown on overlay. Allow the letter E only to mark the point.
4. (b) Overlay (viewed with diagram) (i) angle 103° (ii) angle 42° AC = 15·3 (cm) Must be a line from A cutting the given line through B. Their point of intersection is C. If line is a 'dog leg', use part starting at A to decide the 42° and AC gets B0. Generally, use the overlay to check that their line AC is consistent with their value for AC. Otherwise use measuring tool.		B1 B1 B1	Allow $\pm 2^\circ$ Inclusive bounds are shown on overlay. F.T. their diagram. If their angle is 40° AC = 14.4 (cm) ± 2 mm If their angle is 44° AC = 16.0 (cm) ± 2 mm (Interpolate other angles between 40 – 44) For angles outside this range, use a measuring tool. <u>Note:</u> A straight line drawn from A to end of the line through B, gives AC=16·5 ± 2 mm. and gains the 3 rd B1. (The 42° would be B0).
5. (a) (i) certain (ii) (an) even chance (iii) impossible (iv) unlikely		B1 B1 B1 B1	C.A.O. Accept 'evens' C.A.O. C.A.O.
(b) (i) $\frac{1}{4}$ OR 90/360 (ISW) OR equivalent. (ii) 120/360 of 240 OR $\frac{120 \times 2}{3} = 80$	✓ ✓ ✓ ✓	B2 M1 A1	B1 for sight of $90 \pm 2^\circ$. OR B1 for F.T. their fraction : $\frac{\text{their angle } (85 - 95)}{360}$ Allow $115^\circ - 125^\circ$ F.T. their '115 – 125' (76 – 84) 80/240 gets M1, A0. If they work out C and D separately then M1 for either C or D worked out by a correct method and A1 for BOTH answers correct. (Values for C and D between 38 and 42 inclusive).

Paper 1 (Non calculator) Foundation Tier Summer 2010	✓	Marks	Comments																					
6. A (5, 1) B (-3, 0) C (-2, -3)		B1 B1 B1	C.A.O. C.A.O. C.A.O.	Reverse coordinates gets 0. Allow plots within a 2mm square inclusive. Ignore incorrect labelling. Accept the letters A,B, C instead of points																				
Parts (a) & (b) marked at the same time																								
7. (a) Correct pattern with 8 black and 12 white discs <div style="text-align: center;"> <table border="0"> <tr><td>○</td><td>○</td><td>○</td><td>○</td></tr> <tr><td>○</td><td>●</td><td>●</td><td>●</td><td>●</td><td>○</td></tr> <tr><td>○</td><td>●</td><td>●</td><td>●</td><td>●</td><td>○</td></tr> <tr><td>○</td><td>○</td><td>○</td><td>○</td></tr> </table> </div>	○	○	○	○	○	●	●	●	●	○	○	●	●	●	●	○	○	○	○	○		B1	C.A.O.	
○	○	○	○																					
○	●	●	●	●	○																			
○	●	●	●	●	○																			
○	○	○	○																					
7. (b) 8 10 12 14		B2	B1 for each column. F.T. from 1st column (+2)																					
7. (c) (i) $16/2 = 8$ (ii) $16 + 4$ OR $2 \times 8 + 4 = 20$		M1 A1 M1 A1	C.A.O. F.T. $2 \times$ 'their 8' + 4																					
8. a = 5 b = 2 c = 4 d = 7	✓ ✓ ✓ ✓	B1 B1 B1 B1 4	C.A.O. F.T. $17 - 3 \times$ 'their a' F.T. $[12 - 2 \times$ 'their b']/2 F.T. $18 -$ 'their a+ b +c'																					
9. (a) 47 OR 36 <table border="0" style="width: 100%;"> <tr> <td style="width: 50%; text-align: center;"> $\begin{array}{r} \times 36 \\ 282 \\ \hline 1410 \\ 1692 \\ \hline = 1692 \text{ seats} \end{array}$ </td> <td style="width: 50%; text-align: center;"> $\begin{array}{r} \times 47 \\ 252 \\ \hline 1440 \\ 1692 \\ \hline = 1692 \text{ seats} \end{array}$ </td> </tr> </table>	$\begin{array}{r} \times 36 \\ 282 \\ \hline 1410 \\ 1692 \\ \hline = 1692 \text{ seats} \end{array}$	$\begin{array}{r} \times 47 \\ 252 \\ \hline 1440 \\ 1692 \\ \hline = 1692 \text{ seats} \end{array}$	✓ ✓ ✓	M1 A1 A1	Any correct method for the multiplication of 47 by 36 For either 282 or 1410 OR for 252 or 1440 (Apply 'one error' in other methods) C.A.O. Place value errors get M0, A0																			
$\begin{array}{r} \times 36 \\ 282 \\ \hline 1410 \\ 1692 \\ \hline = 1692 \text{ seats} \end{array}$	$\begin{array}{r} \times 47 \\ 252 \\ \hline 1440 \\ 1692 \\ \hline = 1692 \text{ seats} \end{array}$																							
9. (b) $(1/9 \text{ of } 72) = 8$ $4/9 \text{ of } 72 = 32$		B1 B1	Allow B1 for $4/9 \times 72$ OR $288/9$ OR sight of 8 C.A.O.																					
9. (c) 10		B1	Accept -10																					
10.(a) (i) 19·24 (ii) 19240 (iii) 5·2		B1 B1 B1	C.A.O. C.A.O. C.A.O.																					
10. (b) (i) 1000 (ii) 9·02		B2 B1	B1 for the 8 OR 125 OR 10^3 . B0 for $2 \times 2 \times 2 \times 5 \times 5 \times 5$ C.A.O.																					
10. (c) (i) 6400 (ii) 0·053		B1 B1	C.A.O. C.A.O. 0·05300 etc gets B0																					
11. (a) $360 - 66 - 58 = 236$ 118	✓ ✓ ✓	M1 A1 B1	Any correct method, e.g. using isosceles triangles. F.T. 'their 236' $\div 2$																					
11. (b) S R Q		B1 B1 B1																						

Paper 1 (Non calculator) Foundation Tier Summer 2010	✓	Marks	Comments
All parts (a) – (d) marked at the same time			
12. (a) $\begin{matrix} 6 & 6 \\ 5 & 5 \\ 4 & 5 \\ 4 & 5 \\ 4 & 5 \\ 4 & 5 \end{matrix}$		B2	B1 for any 1 correct column OR B1 for 6, 6 with 5, 5 with any one of the four rows of 4, 5
(b) (i) $5/36$ ISW		B2	F.T. their table B1 for a numerator of 5 in a fraction less than 1. B1 for the 36 in a fraction <1. Do not penalise incorrect reduction of fractions in (b)(i).
(ii) $31/36$ ISW		B1	F.T. 1 – ‘their $5/36$ ’ ($\neq \frac{1}{2}$).
(c) $4/36$ ISW		B1	B0 here if there is incorrect reduction. F.T. consistent use of ‘their 36’
(d) (i) $4/36 \times 360 = 40$		M1 A1	F.T. ‘their (c) $\times 360$ ’ ($\neq \frac{1}{2}$). A0 here if there is incorrect reduction.
(ii) Profit = $360 \times \text{£}1 - 40 \times \text{£}5 = \text{£}160$		M1 A1	F.T. ‘their 40’
13. (a) 2 and 8 in any order 5 in the square and 12.5 in the cross H1		B1 B1	
13. (b) $x + y$ in the circle and xy in the cross H1		B2	B1 for either. Accept $x \times y$ for xy
14. (Viewed with diagram) (a) $120^{(0)}$ H3a		B1	Must be 3 figure bearing
14. (b) $180 + 52$ OR $360 - (180 - 52)$ OR equivalent H3b $232^{(0)}$		M1 A1	
15. (a) $2 \times \pi \times 5$ or equivalent H4a $31.4\dots$ cm		M1 A1	Accept their value of π for M1 Watch for $5^2 = 10$ which gets M0, A0.
15. (b) $\pi \times 10^2$ $314. (\dots \text{cm}^2)$ H4b		M1 A1	Accept their value of π for M1. Needs intention of 10^2 $\pi \times 5^2$ is NOT a misread. It gets M0, A0 $\pi \times r^2 \times 10 \times 10$ gets M0, A0
15. (c) $0.5 \times 2.8 \times (3 + 7)$ $14 (\text{cm}^2)$ H4c		M1 A1	OR equivalent
16. (a) 12.5, 17 and 21.5 H5a	✓	B3	B2 for any 2 correct. B1 for any one correct or sight of 4.5
16. (b) $5n + 3$ OR $5 \times n + 3$ H5d		B2	B1 for $5n$. Accept $5N$, but penalise – 1 for using any other letter.
16. (c) $n \times n$ OR n^2		B1	Accept nn OR (any letter) ² without penalty, B0 for pattern \times pattern etc
17. (a) Method with at least 2 correct prime factors Sight of correct factors (2, 2, 2, 3, 3, 11) $2^3 \times 3^2 \times 11$ or $2^3 \cdot 3^2 \cdot 11$ H6a	✓ ✓ ✓	M1 A1 B1	Starting with 792, two correct primes before 2 nd error. Ignore 1s seen FT their factors (with at least one index >1 used). Do not ignore 1s.
17. (b) e.g. 2×3^2 not even powers, or 2×9 but not square H6b		E1	OR $4 \times 4 = 16$ and $5 \times 5 = 25$ so 18 not square <i>Do not accept “even powers” without relevant working, nor “no number times itself gives 18”. But do accept “no WHOLE number times itself gives 18”.</i>
18. Overlay Correct region shaded Tick outside the region covered by the overlay. H7	✓ ✓ ✓	B3	Mark intention. B1 for line (at least 1cm), B1 for arc (at least 1 cm), B1 for shading (F.T. arc centre A and a line crossing AB) (Shading needs to be on both sides of AB) Note: Arc centre B is MR–1 and continue to mark

NOTES
Penalise –1 for use of words such as “5 out of 36”, “5 in 36” OR “5:36”.
When fraction and wrong notation seen, DO NOT penalise wrong notation.

Mathematics Paper 1 - Higher Tier

Paper 1 (Non- calculator) - Higher Tier Summer 2010	Marks	Comments
1. (a) 2 and 8 in any order 5 in the square and 12.5 in the cross (b) $x+y$ in the circle and xy in the cross	B1 B1 B2 4	B1 for either. Accept xy for xy .
2.(a) Correct reflection (in the line $x=-2$) (b) Correct translation	B2 B2 4	B1 for a reflection in any vertical line, or B1 for drawing $x = -2$, or B1 for reflection in $y=-2$ without line shown. B1 for translation 2 right or 3 up.
3. (a) $3x+20+x+60+x=180$ OR equivalent $x = 20^{(0)}$ $y = 160^{(0)}$ (z =) $3x + 20$ or $3 \times 20 + 20$ $z = 80^{(0)}$ (b) (i) $120^{(0)}$ (ii) $180 + 52$ OR $360 - (180 - 52)$ OR equivalent $232^{(0)}$	M1 A1 B1 M1 A1 B1 M1 A1 8	Award M1 A1 for 20^0 without working FT $180 - x$. <i>SCI</i> $4x+80$ or $3x+20+x+60$ FT from their x For evaluation
4. (a) $2 \times \Pi \times 5$ or equivalent $31.(4\dots \text{cm})$ (b) $\Pi \times 10^2$ $314.(.\text{cm}^2)$ (c) $0.5 \times 2.8 \times (3 + 7)$ $14 (\text{cm}^2)$	M1 A1 M1 A1 M1 A1 6	Accept their value of Π for M1 Accept their value of Π for M1. Needs intention of 10^2 Or equivalent
5. (a) 12.5, 17 and 21.5 (b) -2, 1, 6 (c) (i) -2 (ii) $7(n-5)$ or $7x(n-5)$ or $7n - 35$ ISW (d) $5n + 3$ or $5 \times n + 3$ (e) $n \times n + 1$ or $n^2 + 1$	B3 B2 B1 B2 B2 B2 12	B2 for any 2 correct. B1 for any one correct or sight of 4.5 B1 for any 2 terms correct. <i>SC1</i> for -3, -2, 1 OR 1^2-3 , etc B1 for missing or incorrect brackets, e.g. $n - 5 \times 7$, $7 n - 5$, $n-5(7)$ B1 for $5n$ B1 for sight of n^2 or $n \times n$, must be coefficient 1
6. (a) Method with at least 2 correct prime factors Sight of correct factors (2, 2, 2, 3, 3, 11) $2^3 \times 3^2 \times 11$ or $2^3 \cdot 3^2$. 11 (c) E.g. 2×3^2 not even powers, or 2×9 but not square	M1 A1 B1 E1 4	Starting with 792, 2 correct primes before 2 nd error Ignore 1s seen FT their factors (with at least one index >1 used). Do not ignore 1s. Or $4 \times 4 = 16$ and $5 \times 5 = 25$ so 18 not square <i>Do not accept "even powers" without relevant working, nor "no number times itself gives 18". But do accept "no whole number times itself gives 18"</i>
7. Correct region shaded	B3 3	Mark intention. B1 for line, B1 for arc, B1 for shading (FT arc centre A and a line crossing AB). Shading needs to be on both sides of AB. Remember arc centre B is MR-1 continue to mark
8. (a) $20 + x = 3 \times 7$ OR $20/3 + x/3 = 7$ $x = 3 \times 7 - 20$ OR $x/3 = 7 - 20/3$ $x = 1$ (b) $6x - 2x < 24$ OR $4x < 24$ $x < 6$	B1 B1 B1 B1 B1 5	OR first correct step FT until 2 nd error (a)&(b) Working with $20+x$ incorrectly is 2 errors Or unsimplified equivalent Must be simplified <i>Use of "=" gets 0, unless replaced to finish, then B2</i>
9.(a) -1 (b) Plots correct, allowing one error All points correct & joined with a curve (c) $y = -20$ seen or implied About -1.8	B1 B1 B1 M1 A1 5	FT from (a) FT from (a) FT their graph FT their graph

Paper 1 (Non- calculator) - Higher Tier Summer 2010	Marks	Comments
10.(a) 22 (b) Computer Tronics Reason, e.g. Mode lower, less time, (c) 2, 18, 24, 28 (d) Intention to plot at upper bounds 3 unique vertical plots correct All plots correct and joined (e) (i) Median from cumulative graph (....) (ii) Attempt, (using the reading on the horizontal) UQ - LQ	B1 B1 E1 B1 B1 M1 A1 B1 M1 A1 10	CAO. Now only FT their <u>cumulative table</u> to (d) Ignore bars only if intention clear that line or curve is being used in (e) FT from their cumulative graph in (e) <i>If (c) is not cumulative then do not FT to (d) and (e)</i>
11. Idea that $5s+3b=100$ or $s+b=22$, which maybe via calculations shown or equations Equal coeffs. for simultaneous equations, or trial pairs of values total 22 aiming to make 100 Sara 17 and brother 5	S1 M1 A2 4	Working that meets just one of the two criteria, e.g. any 2 ages with total of 22 A1 for either correct <i>Answers only credit all 4 marks</i>
12. Implied or sight of 2^2 , 4, 3^2 or 9 Considers 2.5^2 Evaluates 2.5^2 to 6.25 Answer 3 given having <u>considered</u> 2.5^2	B1 M1 A1 A1 4	Or 2.5^2 2.5^2 may not have been evaluated correctly <i>SC1 for answer of 3 with spurious or no working</i>
13.(a) All 6 correct entries (b) 0.4×0.3 = 0.12	B3 M1 A1 5	B2 for any 2 correct pairs OR B1 for any 2 correct entries FT their unambiguous entries Or equivalent
14.(a) Alan AND reason given (b) Clive AND reason given (c) 58.9 AND 2.6	B1 B1 B1 3	e.g. "smaller value for SD" E.g. "greater mean" ignore mention of SD. Accept Alan with full explanation mentioning SD & mean
15. (a) 23^0 Alternate segment theorem (b) 67^0 (Isosceles triangle,) angle at centre twice angle at circumference or alternative	B1 E1 B1 E1 4	Accept equal to $A \hat{C} B = A \hat{B} R$ FT if possible Do not accept calculation shown. Accept abbreviations
16. Area scale factor 3^2 or 9 $90 / 9$ $10 \text{ (cm}^2\text{)}$	B1 M1 A1 3	FT for M1 only incorrect evaluation of 3^2 as 6 CAO
17. (a) $(2w + 3)(7w + 1)$ -3/2 and -1/7 (b) $(3e - 7)(3e + 7)$	B2 B1 B2 5	B1 for $(7w \dots 1)(2w \dots 3)$ or split mid term and 1 st step factor F.T. for pair of brackets B1 for $(3e \dots 7)(3e \dots 7)$
18.(a) Reflection (b) Translation to the right Clearly crosses (5, 0) (c) Vertical translation downwards -6	B1 B1 B1 B1 B1 5	Allow SC1 for left shift with 1 indicated. FT from their vertical translation to -4 only. Accept indication on the diagram
19. $(x+3)(x-3) + 3(x+1) = 2(x+1)(x-3)$ $x^2 - 9 + 3x + 3 = 2(x^2 + x - 3x - 3)$ $x^2 - 7x = 0$ $x = 0$ AND $x = 7$	M2 A2 M1 A1 6	M2 for correct numerator/denominator = 2, OR M1 for 2 terms correct, or 1 slip, A1 LHS or numerator, A1 RHS expansion FT for equivalent level of difficulty CAO

Mathematics Paper 2 - Foundation Tier

Paper 2 Foundation Tier (Calculator allowed) Summer 2010	✓	Marks	Comments
Parts (a) & (b) marked at the same time			
1. (a) (56.94) 13.96 (files) 22.08 (post-it) 19.02 (paper) 112(.00) (b) (£) 11.2(0)		B1 B1 B1 B1 B1 5	C.A.O. C.A.O. C.A.O. F.T. their figures for 1 error <u>Unsupported 112(.00) gets B4.</u> F.T. their total <u>(£)100.8(0) gets the B1.</u>
2. kg cm or mm kilometres or km ml or cm ³ or l(itres)	✓ ✓ ✓ ✓	B1 B1 B1 B1 4	kilos gets B0 C.A.O. kilos gets B0 C.A.O. Ignore quantities, e.g. 56kg OR 20cm etc, each get B1
3. (a) radius tangent chord	✓ ✓ ✓	B1 B1 B1	C.A.O. C.A.O. C.A.O.
3. (b) cuboid rhombus trapezium	✓ ✓ ✓	B1 B1 B1	C.A.O. C.A.O. C.A.O.
3. (c) Both lines of symmetry	✓	B2	B1 for either one of them and no incorrect lines. OR for both correct lines and 1 incorrect line.
All parts (a) – (c) marked at the same time			
4. (a) 5, 14, 12, 6, 3 (b) 1 (c) 0, 1, 2, 3, M along one axis OR 0,1,2,3,4 Uniform scale for the frequency axis starting at 0 Five bars at correct heights (ignore widths of bars)		B2 B1 B1 B1 B2 7	B1 for any three/four correct frequencies If frequencies score 0, then give B1 for all 5 correct tallies. F.T. their table of frequencies Accept 1 and 14 but not 14 alone. Anywhere within the base (inc.) of the corresponding bar. If no scale then B0, but allow one square to represent 1. If frequency scale starts with 1 at the top of the first square the starting at 0 will be implied for B1. F.T. their table of frequencies B1 for any 3 or 4 correct bars on F.T.
5. (a) Printing Cost = $300 \times 9 + 2000$ = (£) 4700		M1 A1	C.A.O.
5. (b) Cost per book = $(5000 - 2000) / 600$ = (£) 5		M1 A1	C.A.O. Accept embedded answers.
6. (a) Sum of the numbers (511) Sum / 7 73	✓ ✓ ✓	M1 m1 A1	For attempt to add the numbers (totals of 421 – 601) If seen. C.A.O.
6. (b) 51 53 75 <u>78</u> 81 83 90 Median = 78		M1 A1	For attempting to order the numbers C.A.O.
6. (c) 39		B1	

Paper 2 - Foundation Tier (Calculator allowed) Summer 2010	✓	Marks	Comments
7. Man 5 to 7 ft OR 1.5 to 2.5 metres (Man 1cm Dinosaur = 8cm) Multiplying factor = 8 Estimate height of dinosaur = estimate × factor F.T. their estimates × their SF (5 – 11 inc.) = correct answer for their figures <u>SC1 for answers which:</u> (a) only give man's height as 1cm and dinosaur's as 8cm ± 2mm OR (b) a proper attempt at 'dividing' the dinosaur's height into equal parts	✓ ✓ ✓ ✓	B1 B1 M1 A1 4	Unsupported answers marked as follows: F.T. their man's height estimate AND scale factors 5–11 inc. Correct units must be seen at least once to get the final A1
8. (a) 7/100		B1	C.A.O.
8. (b) 20/84 OR 2000/84 OR 23.8(095..) OR 20/84 = 23 Change = 68p	✓ ✓ ✓	M1 A1 A1	Sight of (£)19.32 gets this M1 C.A.O. Allow A1 for an embedded 23 in their working. F.T. their 23
9. (a) (i) 5 (ii) 22		B1 B2	C.A.O. Watch out for 20 ÷ 5 = 4 which gets B0. B1 for sight of 28 OR 'their 28' – 6
9. (b) Add 7 (to the previous term) Multiply (previous term) by 3		B1 B1	Accept +7 Accept ×3
10. (a) 12 (°C)		B1	C.A.O.
10. (b) -4 (°C)		B1	C.A.O.
10. (c) (+) 7 (°C)		B1	B0 for -7
11. (a) euros = 1200 × 1.27 = (€) 1524		M1 A1	C.A.O. Ignore units
11. (b) Pounds = 486/1.35 = (£) 360		M1 A1	C.A.O. Ignore units. Allow embedded answers
12. (a) 1 - 8		B1 B1	C.A.O. F.T. 'their 1' – 9 if answer is negative.
12. (b) $x = 10/4$ I.S.W. (OR 2½ OR 2.5)		B2	Accept embedded answers such as $4 \times 2\frac{1}{2} - 7 = 3$ F.T. $ax = b$ provided $a \neq 1$ B1 for $4x = 10$
12. (c) $4x + 2y$		B2	B1 for either $4x$ OR $2y$ in an expression of the form $ax \pm by$
13. $23 \times 2 + 24 \times 13 + 25 \times 14 + 26 \times 10 + 27(\times 1)$ OR $46 + 312 + 350 + 260 + 27$ = 995		M1 A1	Not all required, allow 1 error in working shown. C.A.O.
14. (a) $\frac{46}{100} \times 54$ = 24.8(4) OR 25 ISW		M1 A1	C.A.O. Ignore %.
14. (b) $\frac{77}{140} \times 100$ = 55 (%)		M1 A1	C.A.O.

Paper 2 Foundation Tier (Calculator allowed) Summer 2010	✓	Marks	Comments																								
15. (a) Reason, e.g. outside the fish & chip shop H1a		E1	Accept reference to question 2 <i>Ignore additional information given by the candidate once a correct response has been given credit.</i>																								
15. (b) Any 2 of: No under 15s, 30 appears in two boxes, may object to giving their age H1b		E2	E1 for each response. Do not accept: Over 40s in one group, gaps between ages different <i>Ignore additional information given by the candidate once a correct response has been given credit.</i>																								
15. (c) (i) Explanation, e.g. vague, no options, asks 2 questions, same question twice, open questions, can't display answers easily, can't answer if answer to Q2 is NO, many payment methods, not same pattern as Q1 & Q2 (ii) States to give options OR give some options, e.g. card/cash OR deletes 1 question H1c		E1 B1	Do not accept: could be more than one answer <i>Ignore additional information given by the candidate once a correct response has been given credit.</i>																								
16. (a) Volume = $6 \times 4 \times 5$ = 120 cm ³		M1 A1 U1	Independent of the other marks																								
16. (b) $(6 \times 4 + 4 \times 5 + 6 \times 5)$ Area = 2×74 OR $2 \times (6 \times 4 + 4 \times 5 + 6 \times 5)$ = 148 (cm ²)	✓ ✓ ✓	M1 m1 A1	Dependent on the M1 C.A.O.																								
17. (a) Strategy, $\times 2.5$ OR $/4$ then $\times 10$ or equivalent Any 4 correct values seen All values correct <i>Accept 1000g and 2000g written as 1kg and 2kg – units need to be correct</i> H2a	✓ ✓ ✓	M1 A1 A1	<table border="1"> <thead> <tr> <th colspan="4">Ingredients to serve 10 people</th> </tr> <tr> <th colspan="2">For the spaghetti</th> <th colspan="2">For the sauce</th> </tr> </thead> <tbody> <tr> <td>1000g/ 35oz</td> <td>Flour</td> <td>10</td> <td>tblsp olive oil</td> </tr> <tr> <td>10</td> <td>eggs</td> <td>5</td> <td>onions</td> </tr> <tr> <td></td> <td></td> <td>2000g/ 70oz</td> <td>fresh chopped toms.</td> </tr> <tr> <td></td> <td></td> <td>50</td> <td>leaves of fresh basil</td> </tr> </tbody> </table>	Ingredients to serve 10 people				For the spaghetti		For the sauce		1000g/ 35oz	Flour	10	tblsp olive oil	10	eggs	5	onions			2000g/ 70oz	fresh chopped toms.			50	leaves of fresh basil
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17. (b) 3.5 (oz) H2b		B1	C.A.O.																								
18. (a) $7x - 5x = 3 - 2$ $2x = 1$ $x = \frac{1}{2}$ ISW H3a	✓ ✓ ✓	B1 B1 B1	F.T. until 2 nd error F.T. $ax = b$ provided $a \neq 1$																								
18. (b) a^7 H3c		B1	C.A.O.																								
18. (c) $b^2 + 3b$ H3d		B2	B1 for either term correct. Accept $b \times b$ or bb as b^2 , and $b3$ or $3 \times b$ or $b \times 3$ for $3b$. If B2 penalise further incorrect working -1																								
18. (d) $4f = e + 3$ $f = (e + 3)/4$		B1 B1	Isolating the tem in f . Allow B1 for $f = e/4 + 3$																								
19. (a) Any correct 5% of a value used in workings $800 - 5\% \text{ of } 800 (= 800 - 40)$ $760 - 5\% \text{ of } 760 (= 760 - 38)$ (£)722 H6a	✓ ✓ ✓ ✓	B1 M1 M1 A1	OR B1 and M2 for 800×0.95^2 (B1 and M1 for 800×0.95) FT their 760, but not 800 CAO. Penalise extra working -1 Appreciate: Possible B1 and SC1 for (£)882 Simple depreciate: Possible B1 and M1, answer 720 gets B1 M1																								
19. (b) 1 inch as 2.5(4... cm) or 25(4 ... mm) Realising the need to divide by (4×7) Value between 20 and 30 inclusive $\div (4 \times 7)$ correctly evaluated, rounded or truncated H6b	✓ ✓ ✓	B1 B1 B1	If units are given they must be correct <i>SC1 if for value between 20 to 30 inclusive divided by 30 or 31 correctly evaluated, it is also possible to award 1st B1 for 25.</i> <i>A correct answer only of 0.9(mm per day) gets all 3 marks, other values do not</i>																								
20. $3.6^2 + 7.3^2 = AC^2$ $AC^2 = 66.25$ 8 OR 8.1 OR 8.14 (cm) H9	✓ ✓ ✓ ✓	M1 A1 A2	Correct statement (or cosine rule), accept as implied through working FT their AC^2 rounded to whole, 1dp or 2dp if M1 awarded. A1 for $AC = 8.13(9\dots)$																								

Mathematics Paper 2 -Higher Tier

Paper 2 (Calculator allowed) - Higher Tier Summer 2010		Comments
<p>1.(a) Reason, e.g. outside the fish & chip shop</p> <p>(b) Any 2 of: No under 15s, 30 appears in two boxes, may object to giving their age</p> <p>(c) (i) Explanation, e.g. vague, no options, asks 2 questions, same question twice, open questions, can't display answers easily, can't answer if answer to Q2 is NO, many payment methods, not same pattern as Q1 & Q2</p> <p>(ii) States to give options OR give some options, e.g. card/cash OR deletes 1 question</p>	<p>E1</p> <p>E2</p> <p>E1</p> <p>B1 5</p>	<p>Accept reference to question 2</p> <p>E1 for each response. Do not accept: Over 40s in one group, gaps between ages different</p> <p><i>Mark responses in the sections they appear, do not pick out responses in other sections.</i></p> <p><i>In all parts ignore additional information given by the candidate once a correct response has been given credit.</i></p>
<p>2.(a) Strategy, $\times 2.5$ OR $/4$ then $\times 10$ or equivalent</p> <p>Any 4 correct values seen</p> <p>All values correct</p> <p><i>Accept 1000g and 2000g written as 1kg and 2kg – units need to be correct</i></p> <p>(b) 3.5 (oz) CAO</p>	<p>M1</p> <p>A1</p> <p>A1</p> <p>B1 4</p>	<p>Ingredients to serve 10 people</p> <p>For the spaghetti</p> <p>1000g/35oz plain flour</p> <p>10 eggs</p> <p>For the sauce</p> <p>10 tbsp olive oil</p> <p>5 onions</p> <p>2000g/70oz fresh chopped tomatoes</p> <p>50 leaves of fresh basil</p>
<p>3.(a) $7x - 5x = 3 - 2$</p> <p>$2x = 1$</p> <p>$x = \frac{1}{2}$ ISW</p> <p>(b) $8(x + 2)$</p> <p>(c) a^7</p> <p>(d) $b^2 + 3b$</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>B2</p> <p>B1</p> <p>B2</p> <p>8</p>	<p style="text-align: center;">FT until 2nd error</p> <p>FT $ax = b$ provided $a \neq 1$</p> <p>B1 for $4(2x + 4)$ or $2(4x + 8)$</p> <p>B1 for either term correct. Accept $b \times b$ or bb as b^2, and $b3$ or $3 \times b$ for 3b. If B2 penalise further incorrect working -1</p>
<p>4.(a) Uniform scale shown on y axis</p> <p>Any 2 correct points plotted</p> <p>Correct straight line drawn</p> <p>(b) $(3+8)/2$ or $(-1+5)/2$</p> <p>or diagram showing strategy to find mid-point ($5.5, 2$)</p>	<p>B1</p> <p>B2</p> <p>B1</p> <p>M1</p> <p>A2</p> <p>7</p>	<p>Must be shown, but then FT an correct implied scale</p> <p><i>Does not have to start at 0, in which case start value must be seen</i></p> <p>B1 for any 1 correct plot</p> <p><i>Previous B2 maybe implied by sight of a correct line</i></p> <p>The diagram may show horizontal/vertical lines to the axes from points in a sketch.</p> <p>A1 for either. Accept other notation, e.g. missing brackets, $x = 5.5, y = 2$.</p> <p><i>If either coordinate correct do not assume method – check!</i></p> <p><i>(5.5, ...) implies M1 A1 BUT (... , 2) does not imply M1 A1. Check</i></p>
<p>5.(a) All points correctly plotted</p> <p>(b) Line of best fit through Index 73, Arm 66</p> <p>(c) Positive</p> <p>(d) (If no line) answer between 58 and 65 (cm)</p>	<p>B3</p> <p>B2</p> <p>B1</p> <p>B1</p> <p>7</p>	<p>B2 for 5 or 6 points correctly plotted, OR</p> <p>B1 for 3 or 4 points correctly plotted</p> <p><i>SC1 all correctly plotted but joined. Reverse of axes is MR-1</i></p> <p>B1 through means but not reasonable, OR</p> <p>B1 reasonable line not through means</p> <p>Do not accept description</p> <p>FT their line if drawn</p>
<p>6. (a) Any correct 5% of a value used in workings</p> <p>$800 - 5\% \text{ of } 800 (= 800 - 40)$</p> <p>$760 - 5\% \text{ of } 760 (= 760 - 38)$</p> <p>(£)722</p> <p>(b) 1 inch as $2.5(4 \dots \text{cm})$ or $25(4 \dots \text{mm})$</p> <p>Realising the need to divide by (4×7)</p> <p>Value between 20 and 30 inclusive $\div (4 \times 7)$</p> <p>correctly evaluated, rounded or truncated</p>	<p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>7</p>	<p>OR B1 and M2 for 800×0.95^2 (B1 and M1 for 800×0.95)</p> <p>FT their 760, but not 800</p> <p>CAO. Penalise extra working -1</p> <p><i>Appreciate: Possible B1 and SC1 for (£)882</i></p> <p><i>Simple depreciate: Possible B1 and M1, answer 720 gets B1 M1</i></p> <p>If units are given they must be correct</p> <p><i>SC1 for value between 20 to 30 inclusive divided by 30 or 31 correctly evaluated, it is also possible to award 1st B1 for 25.</i></p> <p><i>A correct answer only of 0.9(mm per day) gets all 3 marks, other values do not</i></p>
<p>7. (a) Mid points 155, 160, 165</p> <p>$155 \times 10 + 160 \times 23 + 165 \times 27$</p> <p>$(\sum fx =) 9685$</p> <p>161.4(1666...)</p> <p>(b) Polygon with at least 3 vertices correctly plotted (vertical & horizontal)</p> <p>All 5 vertices of the polygon correct</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>6</p>	<p>FT for their mid points from within group including bounds</p> <p>FT for correct sum of their fx terms</p> <p>FT their $\sum fx / 60$ correct evaluated. Accept 161 from working</p> <p><i>Unsupported 161.4(1666...) awarded 4 marks. FT answer for bounds:(lower 159.4(1666...), upper 163.4(1666...))</i></p> <p>No polygon M0. Ignore bars if polygon drawn</p> <p>Mid points - allow intention to be on lines</p> <p>SC1 for a correct polygon translated horizontally or all correct plots with no polygon (or curved polygon!)</p>

Paper 2 (Calculator allowed) - Higher Tier Summer 2010		Comments								
8. (a) $56.42 / 1.24$ = (£) 45.5(0) (b) Idea 211.50 is 117.5% $211.50 / 117.5 \times 100$ = (£) 180 VAT (£) 31.5(0) “their 31.5(0)” $\times 1.24$ = 39(.06) (Euros) OR correct FT	M1 A1 B1 M1 A1 A1 M1 A1 8	Alternative (b): 211.50×1.24 M1 262.26 (Euros) A1 Idea “their 262.26” is 117.5% B1 $“their 262.26” / 117.5 \times 100$ M1 = 223.2 (Euros) A1 VAT 39(.06) (Euros) A1								
9. $3.6^2 + 7.3^2 = AC^2$ $AC^2 = 66.25$ 8 or 8.1 or 8.14 (cm)	M1 A1 A2 4	Correct statement (or cosine rule), accept as implied through working FT their AC^2 if M1 awarded, rounded to whole or 1dp or 2dp. A1 for $AC = 8.13(9\dots)$ or FT unrounded or truncated answer								
10. $V^2 = PR$ or $V/\sqrt{R} = \sqrt{P}$ $V^2/R = P$ or $(V/\sqrt{R})^2 = P$ or $V^2 \div R = P$	M1 A1 2	Penalise further incorrect working -1								
11. (a) (i) 3.4×10^{-2} (ii) 6×10^6 (b) (i) $3.5(1) \times 10^7$ (ii) $1.7(2\dots) \times 10^{14}$	B1 B1 B2 B2 6	B1 for 35100000 or 35.1×10^6 B1 for $0.17(2) \times 10^{15}$ or correct not in standard form Penalise incorrect notation once only -1								
12. (a) $FG = 17.9 \times \sin 34^\circ$ $FG = 10.(0095\dots)$ (b) $\tan y = 13.2 / 18.7$ = 35(.2\dots) (Accept answers in the range 34.9 to 35.4)	M2 A1 M1 A2 6	M1 for $\sin 34^\circ = FG/17.9$ (or equivalent for sine rule) OR alternative complete method A1 for $\tan y = 0.7(0588\dots)$								
13. (a) $8x + 3y$ (b) $-5x + 9y$	B1 B1 2	Must be in simplest form (a) & (b), no ISW!								
14. (a) $y \propto 1/x$ OR $y = k/x$ $12 = k/2$ $y = 24/x$ <table border="1" data-bbox="164 1106 703 1167"> <tr> <td>x</td> <td>0.1</td> <td>2</td> <td>3</td> </tr> <tr> <td>y</td> <td>240</td> <td>12</td> <td>8</td> </tr> </table>	x	0.1	2	3	y	240	12	8	B1 M1 A1 B2 5	FT non linear only Maybe implied in part (b) FT their non linear expression B1 for each value
x	0.1	2	3							
y	240	12	8							
15. (a) Sight of $x + 5$ (as height) Area = $\frac{1}{2}(x+5)(x+3x+2)$ Convincing step leading to $2x^2 + 11x + 5$ (b) $3x^2 + 11x + 5 = 15$ or equivalent $x = \frac{-11 \pm \sqrt{11^2 - 4 \times 3 \times -10}}{6}$ Allow 1 slip = $\frac{-11 \pm \sqrt{241}}{6}$ 0.75 (cm)	B1 M1 A1 B1 M1 A1 A1 7	or equivalent FT $2x^2 + 11x + 5 = 15$, $x = \frac{-11 \pm \sqrt{11^2 - 4 \times 3 \times -10}}{6}$ Allow 1 slip = $\frac{-11 \pm \sqrt{201}}{6}$ 0.79 (cm) Trial and improvement: M1 2 trials correct between 0.7 & 0.8 A1 Trail 0.754 or 0.755 correct (OR for FT 0.794 or 0.795) A1 0.75 (cm) (OR for FT 0.79 cm)								
16. (a) $BC^2 = 8.6^2 + 6.7^2 - 2 \times 8.6 \times 6.7 \times \cos 140$ $BC^2 = 207.(12896\dots)$ $BC = 14.(3919\dots)$ cm (b) Area = $\frac{1}{2} \times 8.6 \times 6.7 \times \sin 140$ = 18.5(187\dots) cm ² (c) Use of their Area = $\frac{1}{2}$ base \times height, $18.5187\dots = \frac{1}{2} \times 14.39\dots \times \text{ht}$ Height 2.5(73\dots) cm	M1 A1 A1 M1 A1 M1 A1 7	FT their values from (a) & (b)								
17. (a) x^2 horizontal plots at 1, 4, 9, 16 and 25 Plot all points correctly (b) $b = 200 \pm 10$ Use of gradient to find a $a = -8 \pm 2$	B1 B1 B1 M1 A1 5	Allow 1 slip Horizontally & vertically correct Accept graphical or substitution method FT their graph. An answer of 8 ± 2 implies M1								
18. (a) Sin curve, through the origin ± 1 shown, and $\pm 180^\circ$ shown or implied (b) -52° and -128° with no other angles	M1 A1 B2 4	B1 for a correct angle. Accept unrounded values								



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